

Claims

a 1. (currently amended) A method for transforming a message, comprising:
~~represented~~ representing the message as an element of a complete residue set modulo a
prime number p ; a prime number p into a Montgomery residue of a multiplicative inverse, the
method comprising:
selecting a Montgomery radix $R = 2^m$, wherein m is an integer multiple of a wordsize, and
 m is greater than a bit-length of the prime number p ;
determining (r, k) from an almost Montgomery inverse function;
if k is less than m , then assigning r a value obtained as a Montgomery product of r and R^2
 $\text{mod } p$, and assigning k a value $k = k + m$; and
obtaining the multiplicative inverse as a Montgomery product of r and 2^{2m-k} ; and
representing the transformed message as a Montgomery residue of the multiplicative
inverse.

2. (currently amended) A method for transforming a message represented as an element
of a complete residue set modulo a prime number p into a Montgomery residue of a
multiplicative inverse, the method comprising:
selecting a Montgomery radix $R = 2^m$, wherein m is an integer multiple of a wordsize, and
 m is greater than a bit-length of the prime number p ;
determining (r, k) from an almost Montgomery inverse function;
if k is less than m , then assigning r a value obtained as a Montgomery product of r and R^2
 $\text{mod } p$, and assigning k a value $k = k + m$; and
obtaining the multiplicative inverse as a Montgomery product of r and 2^{2m-k} ; and
The method of claim 1, further comprising retrieving a stored value of $R^2 \text{ mod } p$.

3. (previously presented) A computer-readable medium containing instructions for
performing the method of claim 2.

4. (currently amended) A computer-readable medium containing instructions for
performing ~~the method of claim 1~~ a method of transforming a message represented as an element

of a complete residue set modulo a prime number p into a Montgomery residue of a multiplicative inverse, wherein the method comprises:

selecting a Montgomery radix $R = 2^m$, wherein m is an integer multiple of a wordsize, and m is greater than a bit-length of the prime number p ;

determining (r, k) from an almost Montgomery inverse function;

if k is less than m , then assigning r a value obtained as a Montgomery product of r and R^2 mod p , and assigning k a value $k = k + m$; and

obtaining the multiplicative inverse as a Montgomery product of r and 2^{2m-k} .

a!

5. (previously presented) A cryptographic system for encryption and decryption, the system comprising a module for transforming a message as recited in claim 1.

6. (currently amended) A method for transforming a message represented as an element of a complete residue set modulo a prime number p into a Montgomery residue of a multiplicative inverse, the method comprising:

selecting a Montgomery radix $R = 2^m$, wherein m is an integer multiple of a wordsize, and m is greater than a bit-length of the prime number p ;

determining (r, k) from an almost Montgomery inverse function;

if k is less than m , then assigning r a value obtained as a Montgomery product of r and R^2 mod p , and assigning k a value $k = k + m$; and

obtaining the multiplicative inverse as a Montgomery product of r and 2^{2m-k} .

~~The method of claim 1,~~ wherein the message is a ciphertext.

7. (currently amended) A method for obtaining a classical inverse of a message, comprising:

assigning a ~~represented as a series of binary digits to the message,~~ wherein the assigned binary digits represent ~~that is an element of a residue set modulo a prime number p~~ a prime number p ; ~~the method comprising:~~

obtaining values (r, k) by calculating an almost Montgomery inverse function of the representation of the message using a Montgomery radix $R = 2^m$, wherein m is an integer multiple of a wordsize and is greater than a bit-length of the prime number p ;

if k is greater than m , then assigning r a value equal to a Montgomery product of r and 1, and assigning k a value of $k - m$; and

calculating the classical inverse as a Montgomery product of r and 2^{m-k} .

8. (previously presented) A cryptographic system, comprising an encryption/decryption module that performs the method of claim 7.

9. (previously presented) The cryptographic system of claim 8, further comprising at least one integrated circuit.

10. (previously presented) A computer-readable medium, comprising instructions for performing the method of claim 7.

11. (currently amended) A cryptographic method, comprising:
representing a message as a series of binary digits, the series being divisible into an integer number m of words;
selecting a prime number p ;
obtaining an intermediate product r and an integer k using an almost Montgomery inverse procedure, wherein a Montgomery radix $R = 2^m$, and m is greater than a bit-length of the prime number p ;

if $k < m$, then assigning r a value obtained as a Montgomery product of r and $R^2 \bmod p$, and assigning k a value of $k + m$;

retrieving a stored value of $R^2 \bmod p$;

assigning r a value obtained as a Montgomery product of r' and $R^2 \bmod p$; and

obtaining a multiplicative inverse as a Montgomery product of r and 2^{2m-k} .

12. (cancelled)

13. (currently amended) A computer-readable medium containing instructions for performing ~~the method of claim 12~~ a cryptographic method, the method comprising:
representing a message as a series of binary digits, the series being divisible into an integer number m of words;

selecting a prime number p ;

obtaining an intermediate product r and an integer k using an almost Montgomery inverse procedure, wherein a Montgomery radix $R = 2^m$, and m is greater than a bit-length of the prime number p ;

if $k < m$, then assigning r a value obtained as a Montgomery product of r and $R^2 \bmod p$, and assigning k a value of $k + m$;

assigning r a value obtained as a Montgomery product of r' and $R^2 \bmod p$; and

obtaining a multiplicative inverse as a Montgomery product of r and 2^{2m-k} .

14. (currently amended) A method for computing a classical inverse of a message a , the method comprising:

representing the message as a series of bits'

(a) selecting an integer m that is greater than a bit-length of the message a , and selecting a Montgomery radix $R = 2^m$;

(b) selecting a prime number p ;

(c) dividing the series of binary digits representing the message a as a series of binary digits, the series being divided into m words;

(d) obtaining a value $r = a^{-1} 2^m \pmod{p}$;

(e) obtaining the classical inverse as a Montgomery product of r and 1; and

storing the classical inverse of the message in a computer readable medium.

15. (currently amended) A method for computing a classical inverse of a message a , the method comprising:

determining a bit length of a binary representation of the message a ;

(a) selecting an integer m that is greater than $[a]$ the bit-length of the message a , and selecting a Montgomery radix $R = 2^m$;

(b) selecting a prime number p ;
(e) representing the message a as a series of binary digits, the series being divided into m words;

(d) obtaining a value r as a Montgomery product of the message a and $R^2 \bmod p$; and
(e) obtaining the classical inverse as a Kaliski inverse of r ; and
storing the classical inverse of the message in a computer readable medium.

16. (currently amended) A method for computing a multiplicative inverse of an M-residue $A = a2^m \bmod p$, wherein p is a prime number, m is an integer, and a Montgomery radix $R = 2^m$, the method comprising:

computing an intermediate product r and an integer k using an almost Montgomery inverse procedure;

retrieving a value of $R^2 \bmod p$;

assigning an intermediate product r' the value of a Montgomery product of r and R^2 ; and
obtaining the multiplicative inverse as a Montgomery product of r' and 2^{2m-k} .

17. (currently amended) The method of claim 16, further comprising:

determining if the integer k is greater than or equal to m ; and

if the integer k is greater than or equal to m , assigning the intermediate product r' the value of a Montgomery product of r and R^2 and assigning k a value of $k + m$ prior to obtaining the step of obtaining the multiplicative inverse.

18. (cancelled)

19. (currently amended) A computer-readable medium containing instructions for performing the method of ~~claim 18~~ claim 16.

20. (currently amended) A cryptographic method for processing a series of binary digits divided into an integer number m of words, the method comprising:

selecting a Montgomery radix $R = 2^m$ and a prime number p ;

executing an almost Montgomery inverse procedure to obtain an intermediate value r and
an integer k ; and

obtaining a Montgomery product of r ; and

storing the Montgomery product in a computer readable medium.

21. (cancelled)
